

Laws of Logic

- L1. $\neg\neg p \Leftrightarrow p$ Law of Double Negation
- L2. $\neg(p \vee q) \Leftrightarrow \neg p \wedge \neg q$
 $\neg(p \wedge q) \Leftrightarrow \neg p \vee \neg q$ DeMorgan's Laws
- L3. $p \vee q \Leftrightarrow q \vee p$
 $p \wedge q \Leftrightarrow q \wedge p$ Commutative Laws
- L4. $p \vee (q \vee r) \Leftrightarrow (p \vee q) \vee r$
 $p \wedge (q \wedge r) \Leftrightarrow (p \wedge q) \wedge r$ Associative Laws
- L5. $p \vee (q \wedge r) \Leftrightarrow (p \vee q) \wedge (p \vee r)$
 $p \wedge (q \vee r) \Leftrightarrow (p \wedge q) \vee (p \wedge r)$ Distributive Laws
- L6. $p \vee p \Leftrightarrow p$
 $p \wedge p \Leftrightarrow p$ Idempotent Laws
- L7. $p \vee F_0 \Leftrightarrow p$
 $p \wedge T_0 \Leftrightarrow p$ Identity Laws
- L8. $p \vee \neg p \Leftrightarrow T_0$
 $p \wedge \neg p \Leftrightarrow F_0$ Inverse Laws
- L9. $p \vee T_0 \Leftrightarrow T_0$
 $p \wedge F_0 \Leftrightarrow F_0$ Domination Laws
- L10. $p \vee (p \wedge q) \Leftrightarrow p$
 $p \wedge (p \vee q) \Leftrightarrow p$ Absorption Laws
- L11. $p \leftrightarrow q \Leftrightarrow (p \rightarrow q) \wedge (q \rightarrow p)$
- L12. $p \rightarrow q \Leftrightarrow \neg p \vee q$
- L13. $p \rightarrow q \Leftrightarrow \neg q \rightarrow \neg p$

Rules of Inference

- R1. $\frac{p \quad p \rightarrow q}{\therefore q}$ Modus Ponens
- R2. $\frac{p \rightarrow q \quad q \rightarrow r}{\therefore p \rightarrow r}$ Law of the Syllogism
- R3. $\frac{p \rightarrow q \quad \neg q}{\therefore \neg p}$ Modus Tollens
- R4. $\frac{p \quad q}{p \wedge q}$ Rule of Conjunction
- R5. $\frac{p \vee q \quad \neg p}{\therefore q}$ Rule of Disjunctive Syllogism
- R6. $\frac{\neg p \rightarrow F_0}{\therefore p}$ Rule of Contradiction
- R7. $\frac{p \wedge q}{\therefore p}$ Rule of Conjunctive Simplification
- R8. $\frac{p \quad \therefore p \vee q}{\therefore p \vee q}$ Rule of Disjunctive Amplification
- R9. $\frac{p \wedge q \quad p \rightarrow (q \rightarrow r)}{\therefore r}$ Rule of Conditional Proof
- R10. $\frac{p \rightarrow r \quad q \rightarrow r}{\therefore (p \vee q) \rightarrow r}$ Rule for Proof by Cases
- R11. $\frac{p \rightarrow q \quad r \rightarrow s \quad p \vee r}{\therefore (q \vee s)}$ Rule of the Constructive Dilemma
- R12. $\frac{p \rightarrow q \quad r \rightarrow s \quad \neg q \vee \neg s}{\therefore \neg p \vee \neg r}$ Rule of the Destructive Dilemma

Exem Axem [x=0]

Aanvullende wetten m.b.t. quantoren

$$\text{N1. } \neg[\forall x p(x)] \Leftrightarrow \exists x \neg p(x)$$

$$\text{N2. } \neg[\exists x p(x)] \Leftrightarrow \forall x \neg p(x)$$

Aanvullende afleidingsregels m.b.t. quantoren

$$\text{U1. } \frac{\forall x p(x)}{\therefore p(c)} \quad \text{voor een willekeurige } c \text{ in het universum}$$

$$\text{U2. } \frac{\exists x p(x)}{\therefore p(c)} \quad \text{voor een zekere } c \text{ in het universum}$$

$$\text{U3. } \frac{p(c)}{\therefore \forall x p(x)} \quad \text{voor een willekeurige } c \text{ in het universum}$$

$$\text{U4. } \frac{p(c)}{\therefore \exists x p(x)} \quad \text{voor een zekere } c \text{ in het universum}$$

U1: Rule of Universal Specification

U2: Rule of Existential Specification

U3: Rule of Universal Generalization

U4: Rule of Existential Generalization